

6.13 Day 2

Always remember...

LOGS are EXPONENTS !!!

Exponential Form

$$\text{power} \rightarrow y = b^x \leftarrow \text{exponent}$$

↑  
base

Log Form

$$\log_b y = x \leftarrow \text{exponent}$$

↑  
base

① Convert from exponential to log form:

a)  $m = n^p$   
 $\log_n m = p$

b)  $k = j^h$   
 $\log_j k = h$

c)  $32 = 2^5$   
 $\log_2 32 = 5$

② Convert from log to exponential form.

a)  $\log_2 8 = x$   
 $8 = 2^x$

b)  $\log_5 125 = x$   
 $125 = 5^x$

c)  $\log_3 \left(\frac{1}{9}\right) = x$   
 $3^x = \frac{1}{9}$

③ Simplify. Evaluate when possible.

a)  $\log_3 9 + \log_3 27$   
 $2 + 3$   
⑤

b)  $\log_2 8 - \log_2 4$   
 $3 - 2$   
①

$$\begin{aligned} \text{c) } \log_5 25 + \log_5 5 \\ 2 + 1 \\ \textcircled{3} \end{aligned}$$

$$\begin{aligned} \text{d) } \log_2 64 - \log_2 8 \\ 6 - 3 \\ \textcircled{3} \end{aligned}$$

You Try!

$$\begin{aligned} \text{e) } \log_2 8 + \log_4 16 - \log_2 16 \\ 3 + 2 - 4 \\ \textcircled{1} \end{aligned}$$

$$\begin{aligned} \text{f) } \log_3 81 - \log_3 27 - \log_3 3 \\ 4 - 3 - 1 \\ \textcircled{0} \end{aligned}$$

$$\begin{aligned} \text{g) } 2 \log_5 625 + \log_{865} 1 \\ 2(4) + 0 \\ 8 + 0 \\ \textcircled{8} \end{aligned}$$

$$\text{h) } -\frac{1}{2} \log_5 25 + \frac{1}{3} \log_{10} 1000$$

$$-\frac{1}{2}(2) + \frac{1}{3}(3)$$

$$\begin{array}{c} -1 \quad +1 \\ \textcircled{0} \end{array}$$

i)  $\frac{1}{2} \log_5 5 + \log_5 \sqrt[4]{5}$

$$\frac{1}{2}(1) + \log_5 5^{1/4} = x$$

$$\frac{1}{2} + \frac{1}{4}$$

$$\frac{3}{4}$$

④ Solve for x.

a)  $\log_2 x = 4$

$$2^4 = x$$

$$\textcircled{16 = x}$$

b)  $\log_5 x = 3$

$$5^3 = x$$

$$\textcircled{125 = x}$$

⑤ Approximate the solutions to the following equations:

a)  $5^x = 27$       x is between 2 and 3 but is closer to 2

b)  $3^x = 42$

$$3 < x < 4$$

c)  $10^x = 300$

$$2 < x < 3$$

d)  $\log_2 17 = x$

e)  $\log_2 \frac{1}{5} = x$

$$d) \log_2 17 = x$$

$$2^x = 17$$

$$4 < x < 5$$

$$e) \log_2 \frac{1}{5} = x$$

$$2^x = \frac{1}{5}$$

$$-3 < x < -2$$

$$f) \log_4 57 = x$$

⑥ Find the exact solutions to the following equations using your calculator. Round to the nearest hundredth.

$$a) \frac{3 \cdot 4^{x-2}}{3} = \frac{18}{3}$$

$$\underbrace{4^{x-2}}_{y_1} = \underbrace{6}_{y_2}$$

Find intersection:  
2<sup>nd</sup> Trace  
#5 Intersection

$$x \approx 3.29$$

$$b) 2^x - 6 = 3x + 5$$

$$x \approx 4.63$$

$$x \approx -3.64$$

$$c) 8x = 7 \log_{10} 3$$

$$d) \quad -\frac{2}{5}x = 6 - \log 19$$

$$e) \quad \log 10,000 = -x$$